

1 Solutions de l'exercice 1

Notations : On notera $f'(x) = \frac{d}{dx}f(x)$ (notation différentielle de Leibniz)

1. $\frac{d}{dx}(1 - 2x + x^2) = 2x - 2$
2. $\frac{d}{dx}(2x + 1)(x - 3) = 4x - 5$
3. $\frac{d}{dx} \frac{1}{x^2 + 1} = -2 \frac{x}{(x^2 + 1)^2}$
4. $\frac{d}{dx} \frac{2}{x + 3} = -\frac{2}{(x + 3)^2}$
5. $\frac{d}{dx}(x^2 + 1)^3 = 6x(x^2 + 1)^2$
6. $\frac{d}{dx}(2x + 1)^2(x - 3)^3 = (2x + 1)(10x - 9)(x - 3)^2$
7. $\frac{d}{dx} \frac{2x + 1}{x - 2} = \frac{-5}{(x - 2)^2}$
8. $\frac{d}{dx} \frac{x^2 + 2x - 3}{x^2 + x + 1} = \frac{-x^2 + 8x + 5}{(x^2 + x + 1)^2}$
9. $\frac{d}{dx} \frac{(x + 1)^3}{x^2 + 1} = \frac{(x + 1)^2(x^2 - 2x + 3)}{(x^2 + 1)^2}$
10. $\frac{d}{dx} \left(x^2 + x + \sqrt{x} + \frac{1}{x} + \sqrt{2} \right) = 2x + 1 + \frac{1}{2\sqrt{x}} - \frac{1}{x^2}$

2 Solutions de l'exercice 2

1. $\frac{d}{dx}(2 - x + 3x^2) = 6x - 1$
2. $\frac{d}{dx}(2x - 3)(x + 1) = 4x - 1$
3. $\frac{d}{dx} \frac{1}{1 - x^2} = \frac{2x}{(1 - x^2)^2}$
4. $\frac{d}{dx} \frac{3}{x + 2} = -\frac{3}{(x + 2)^2}$
5. $\frac{d}{dx}(1 - x^2)^4 = -8x(1 - x^2)^3$
6. $\frac{d}{dx}(2x - 3)^2(x + 1)^3 = 5(2x - 1)(2x - 3)(x + 1)^2$
7. $\frac{d}{dx} \frac{x - 2}{2x + 1} = \frac{5}{(2x + 1)^2}$
8. $\frac{d}{dx} \frac{x^2 - 2x - 3}{x^2 - x + 1} = \frac{x^2 + 8x - 5}{(x^2 - x + 1)^2}$
9. $\frac{d}{dx} \frac{(1 - x)^3}{1 + x^3} = \frac{-3(x - 1)^2(x^2 + 1)}{(x^3 + 1)^2}$
10. $\frac{d}{dx} \left(x^3 - x - \sqrt{x} - \frac{1}{x} + \sqrt{3} \right) = 3x^2 - 1 - \frac{1}{2\sqrt{x}} + \frac{1}{x^2}$